

Development Accounting

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STEG Lecture

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- ① Income differences across countries
- ② The role of inputs (physical capital and human capital)
- ③ Sources of residual TFP differences
- ④ Welfare vs. GDP

Key citations

- Caselli (2005 Handbook of Economic Growth)
- Caselli and Feyrer (2007 Quarterly Journal of Economics)
- Restuccia and Rogerson (2008 Review of Economic Dynamics)
- Hsieh and Klenow (2009 Quarterly Journal of Economics)
- Hsieh and Klenow (2014 Quarterly Journal of Economics)
- Jones and Klenow (2016 American Economic Review)
- Jones (2016 Handbook of Macroeconomics)
- Boppart and Klenow (2024 Growth chapter in Grad Macro textbook)

PPP GDP for country j based on the sum of expenditures across I goods:

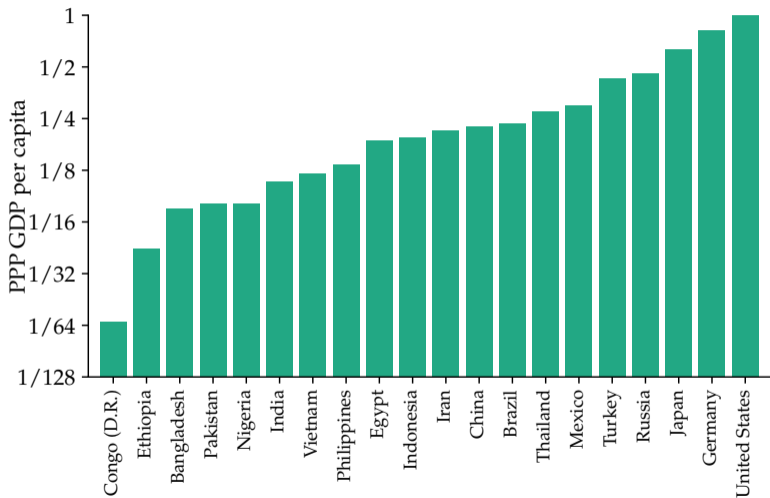
$$Y_j = \sum_i^I P_{i,\text{world}} \cdot Y_{i,j}$$

where $P_{i,\text{world}}$ is a weighted average of $P_{i,j}$ across all countries with weights $Y_{i,j}$.

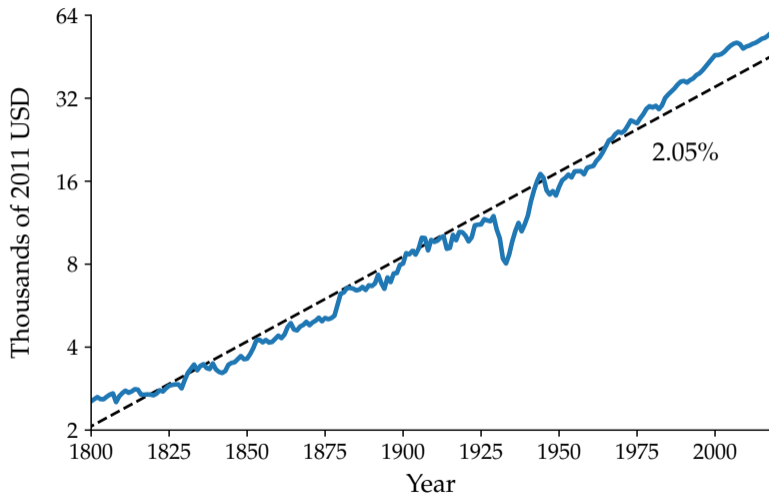
PPP prices tilt toward rich country prices, making poor countries appear richer.

All figures below are based on the latest version, Penn World Table (PWT) 10.01.

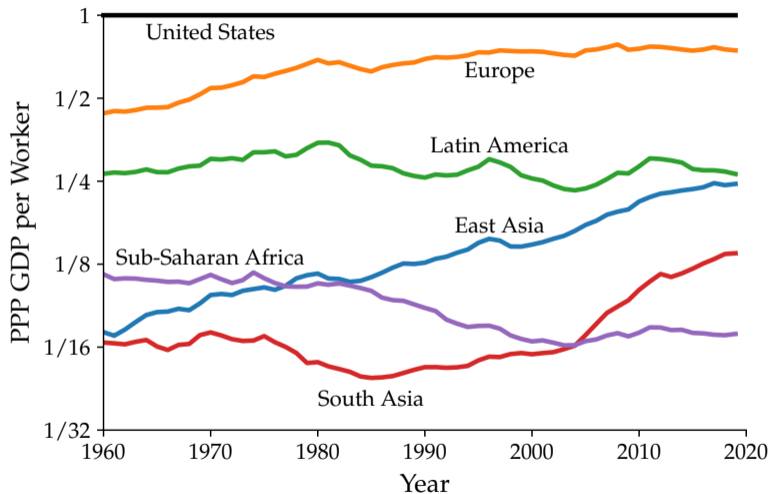
PPP GDP per capita in 2019 (USA=1)



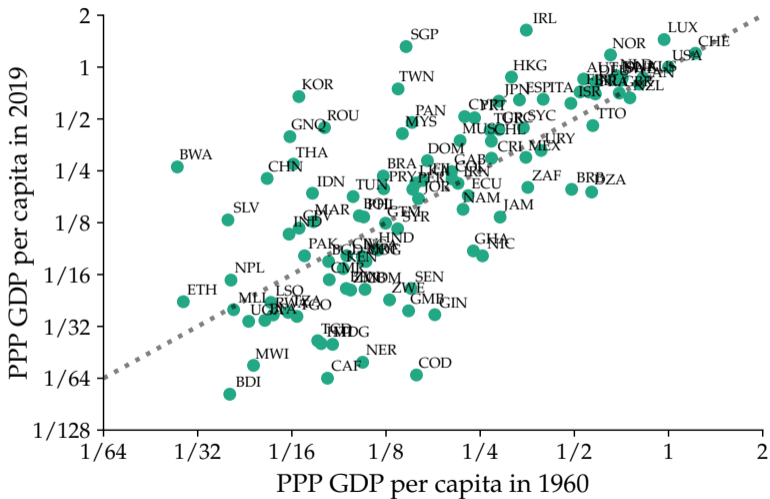
U.S. real GDP per capita, 1800-2023



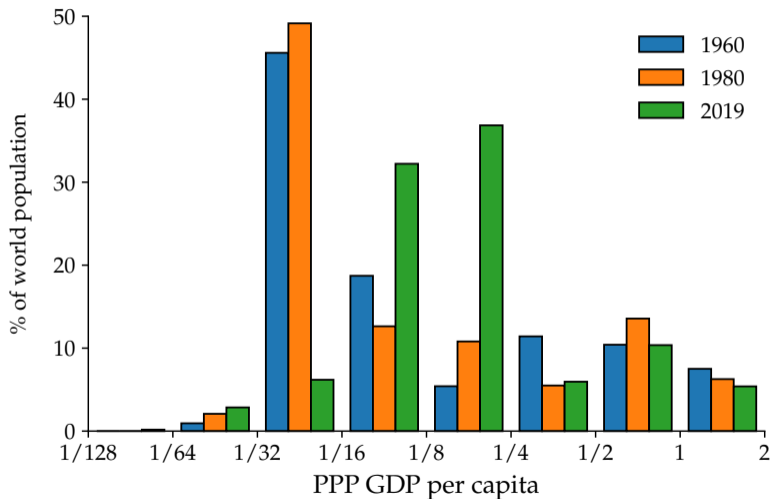
PPP GDP per worker (USA = 1)



PPP GDP per capita in 1960 and 2019 (USA=1 in each year)



PPP GDP per capita in 1960, 1980, and 2019 (USA=1 in each year)



A benchmark production function

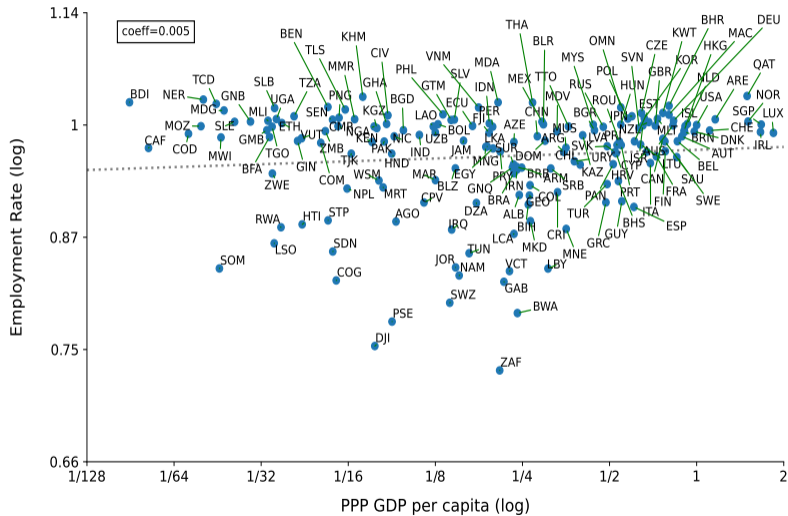
$$Y = K^\alpha (AhL)^{1-\alpha}$$

- Y = PPP GDP
- L = hours worked
- K = PPP physical capital
- h = human capital per worker
- A = a residual
- α = elasticity of output wrt capital

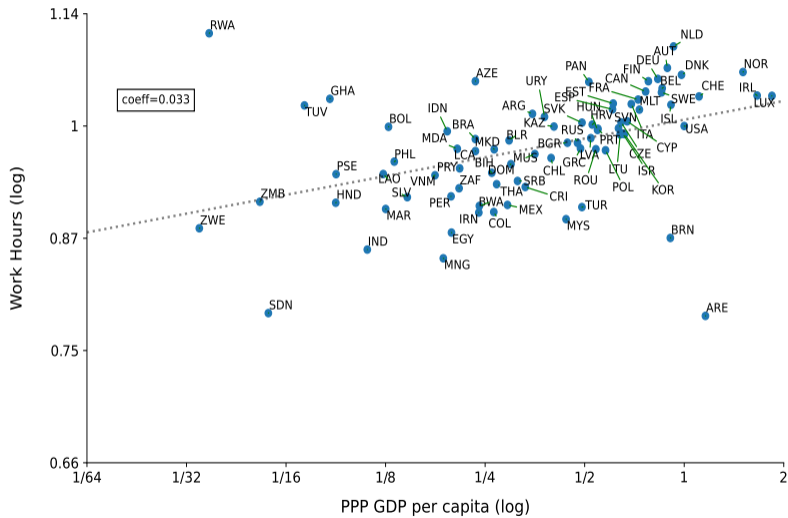
$$\frac{Y}{pop} = \frac{L}{pop} \cdot \left[\frac{K}{Y} \right]^{\frac{\alpha}{1-\alpha}} \cdot A \cdot h$$

- Respects that K/Y is invariant to the other terms in steady state
- Allows h production to be intensive in h

Employment/ Population



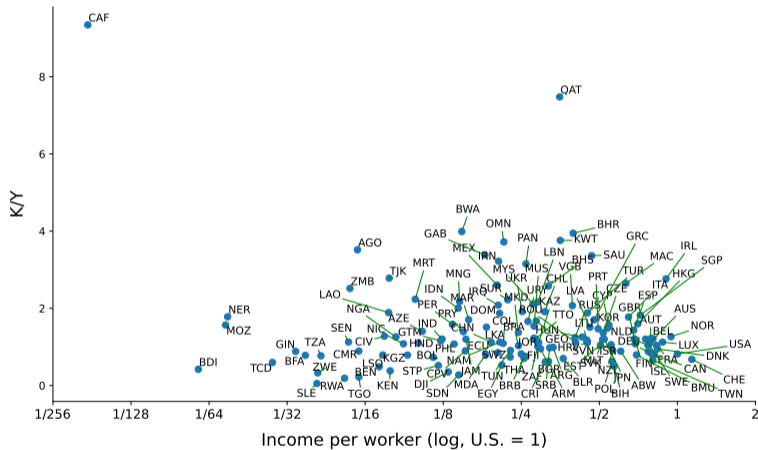
Hours worked per worker



90th/10th percentile country values in 2019:

$$\underbrace{\frac{Y}{pop}}_{12} = \underbrace{\frac{L}{pop}}_{1.1} \cdot \left[\frac{K}{Y} \right]^{\frac{\alpha}{1-\alpha}} \cdot h \cdot A$$

Capital/Output ratios



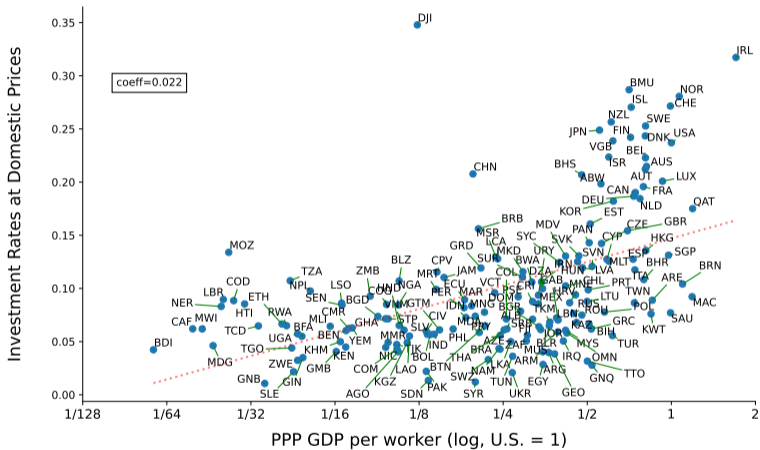
$$\underbrace{\frac{Y}{pop}}_{1.2} = \underbrace{\frac{L}{pop}}_{1.1} \cdot \underbrace{\left[\frac{K}{Y} \right]^{\frac{\alpha}{1-\alpha}}}_{1.4} \cdot h \cdot A$$

Saving rates? YES

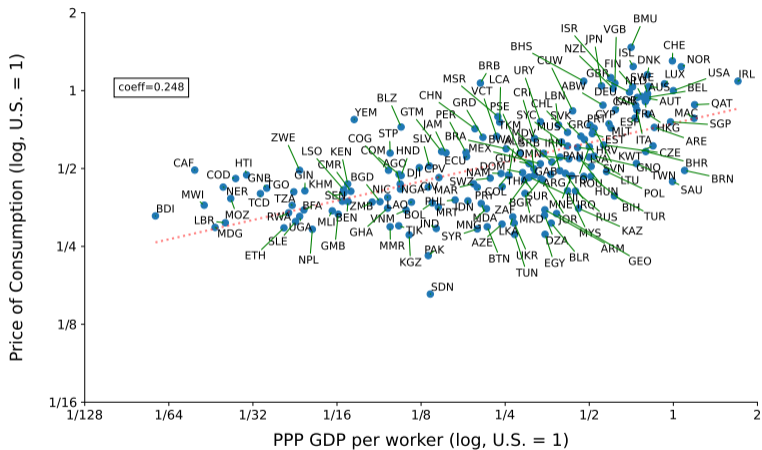
Investment prices? NO

Consumption prices? YES

Investment rates at domestic prices



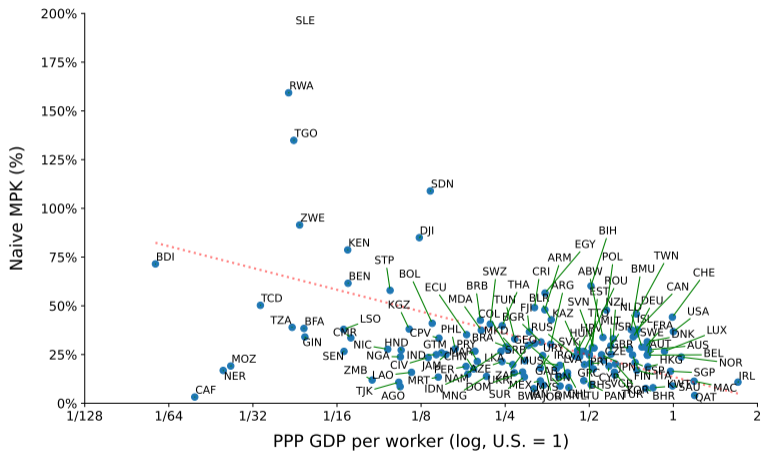
Price of consumption relative to that in the U.S.



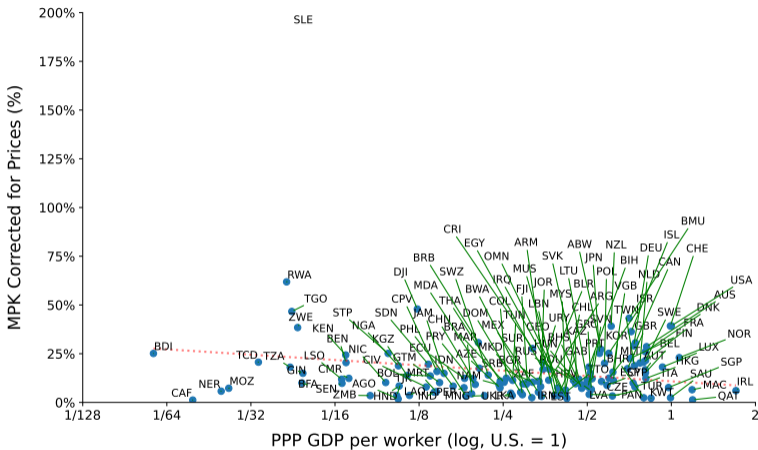
$$\text{Naive MPK} \equiv \frac{\alpha Y}{K}$$

$$\text{Corrected for prices MPK} \equiv \frac{\alpha P_Y Y}{P_K K}$$

Naive MPK



MPK corrected for prices



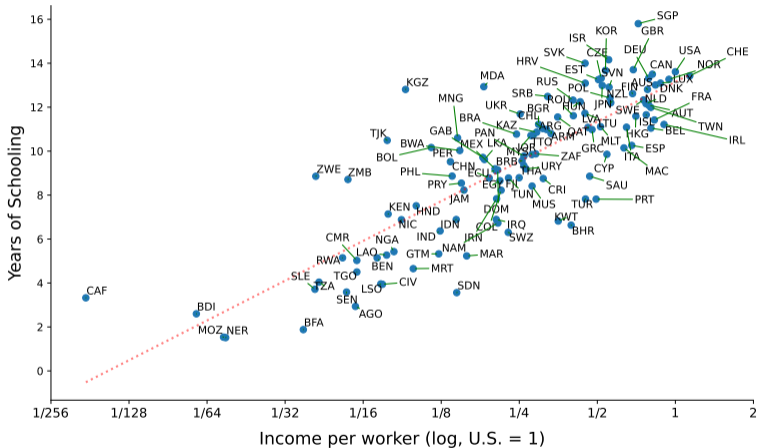
PWT estimates human capital per worker h based on coefficients from regressing log wages on years of schooling across workers within countries (i.e., Mincer regressions):

$$h = e^{\phi(s)}$$

where

$$\phi(s) = \begin{cases} 0.134 \cdot s & \text{if } s \leq 4 \\ 0.134 \cdot 4 + .101 \cdot (s - 4) & \text{if } 4 \leq s \leq 8 \\ 0.134 \cdot 4 + .101 \cdot 4 + 0.068 \cdot (s - 8) & \text{if } s > 8 \end{cases}$$

Years of schooling



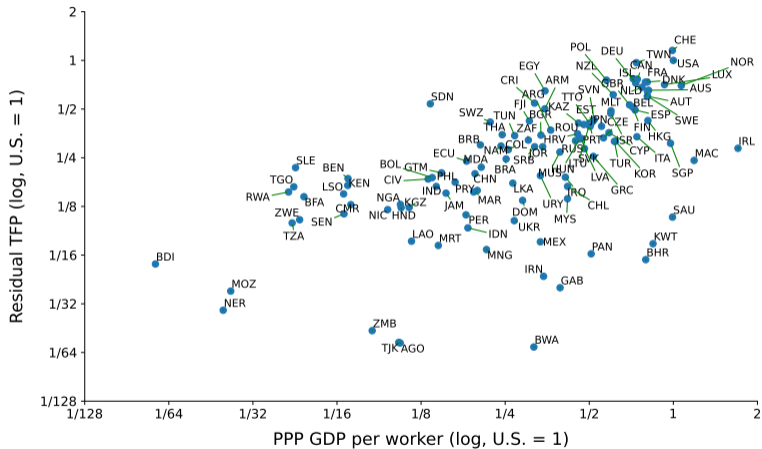
$$\underbrace{\frac{Y}{pop}}_{1.2} = \underbrace{\frac{L}{pop}}_{1.1} \cdot \underbrace{\left[\frac{K}{Y} \right]^{\frac{\alpha}{1-\alpha}}}_{1.4} \cdot \underbrace{h}_{1.7} \cdot \underbrace{A}_{4.9}$$

Development Accounting with all countries

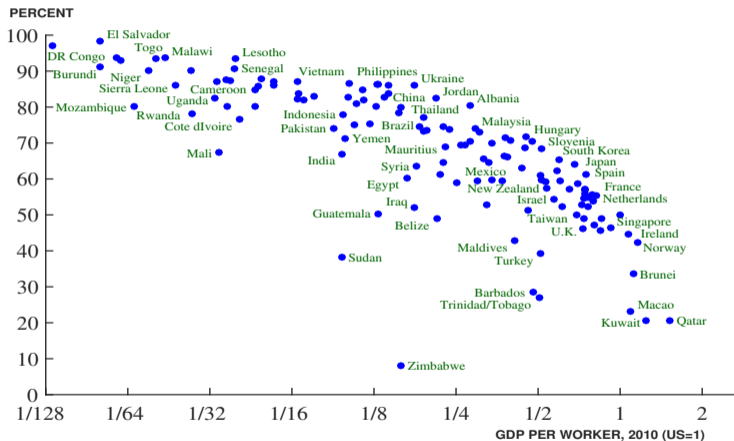
Statistic	Contributions from			
	Y/L	K/Y	h	A
Variance	1.00	0.14	0.08	0.57
Elasticity		0.14	0.22	0.64
90/10 ratio	12.0	1.40	1.70	4.92

Notes: The sample is 117 countries in 2019. The variances are for each variable in logs. The elasticity entries are from separate regressions of each variable on log GDP per capita.

Residual TFP



The Share of TFP in Development Accounting



Limits to the Mincerian schooling approach

- Erosa, Koreshkova and Restuccia (2010 Review of Economic Studies)
- Schoellman (2012 Review of Economic Studies)
- Hendricks and Schoellmann (2018 Quarterly Journal of Economics)
- Lagakos, Moll, Porzio, Qian and Schoellman (2018 Journal of Political Economy)

$$\underbrace{\frac{Y}{pop}}_{1.2} = \underbrace{\frac{L}{pop}}_{1.1} \cdot \underbrace{\left[\frac{K}{Y} \right]^{\frac{\alpha}{1-\alpha}}}_{1.4} \cdot \underbrace{h}_{1.7-5.1} \cdot \underbrace{A}_{1.6-4.9}$$

Potential sources of TFP differences

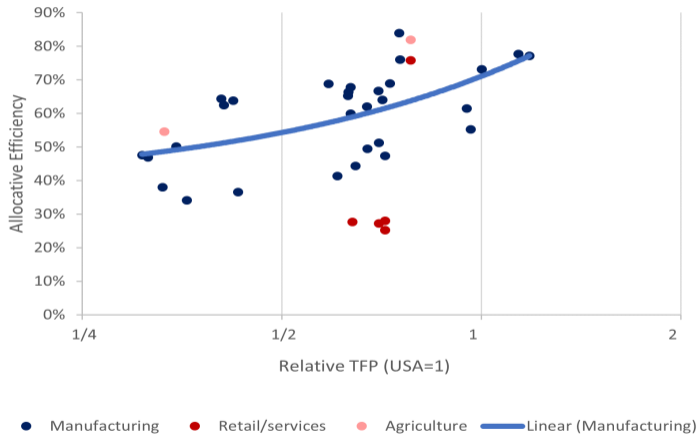
- Technology
- Misallocation
- Natural resources
- Measurement error

- TFPR \equiv revenue/inputs
- Big TFPR gaps exist across firms, even within narrow industries.
- TFPR gaps imply VMPK and VMPL gaps.
- If so, potential aggregate TFP gains from reallocating K and L across firms.

TFPR dispersion within 4-digit industries

	90 th /10 th	75 th /25 th
U.S.	1.9	1.3
China	5.6	2.5
India	5.7	2.4

Allocative Efficiency vs. TFP across 30 countries



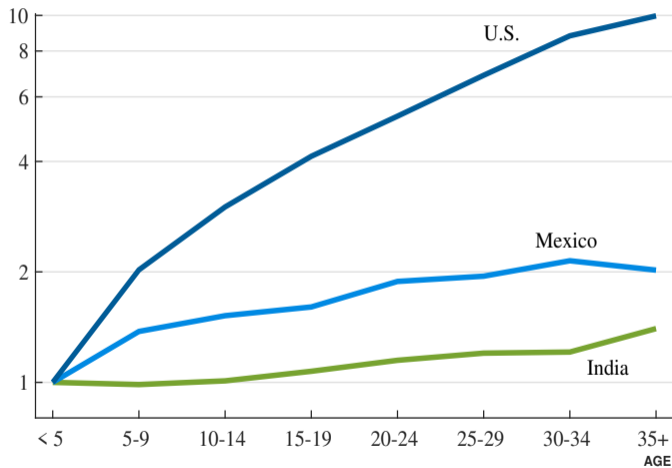
Elasticity of 0.40 (s.e. 0.11) so 40% of TFP differences?

Caveats:

- TFP is for the whole economy
- Varying sample frames (typically broader coverage in rich countries)
- These all use EoS across firms of 3, which is conservatively low
- Measurement error could be worse in poorer countries
- Too few studies for agriculture, services, retail trade

One aspect of technology: firms over their life cycle

AVERAGE EMPLOYMENT (AGE<5 = 1, LOG SCALE)



$$U_0 = E_0 \left[\sum_{a=1}^{100} S(a) \cdot u(c_a, l_a) \right]$$

- U_0 is expected discounted utility
- $S(a)$ is the survival rate through age a and let $e \equiv \sum_{a=1}^{100} S(a)$
- $u(c_a, l_a)$ is flow utility
- c_a is consumption at age a
- l_a is leisure at age a

$$u(c, \ell) = \bar{u} + \log(c) + v(\ell)$$

$$\text{where } v(\ell) = -\frac{\theta\epsilon}{1+\epsilon} \cdot (1-\ell)^{\frac{1+\epsilon}{\epsilon}}$$

- Death is normalized to zero
- ϵ is the constant Frisch elasticity of labor supply
- Assume $\log(c_a) \sim N(\mu, \sigma^2)$ and let $\bar{c} \equiv E(c)$

A decomposition of consumption-equivalent welfare

$$U(e_{us}, \lambda_i \cdot \bar{c}_{us}, \bar{\ell}_{us}, \sigma_{us}) = U(e_i, \bar{c}_i, \bar{\ell}_i, \sigma_i)$$

\Rightarrow

$$\begin{aligned} \log \lambda_i = & \frac{e_i - e_{us}}{e_{us}} \left(\bar{u} + \log \bar{c}_i + v(\bar{\ell}_i) - \frac{1}{2} \sigma_i^2 \right) && \text{Life expectancy} \\ & + \log \bar{c}_i - \log \bar{c}_{us} && \text{Consumption} \\ & + v(\bar{\ell}_i) - v(\bar{\ell}_{us}) && \text{Leisure} \\ & - \frac{1}{2} (\sigma_i^2 - \sigma_{us}^2) && \text{Inequality} \end{aligned}$$

Parameter values:

- $\ln c$ so $\gamma = 1$
- Frisch elasticity of $\epsilon = 1$
- Weight on leisure θ to fit l_{us} , incorporating marginal tax rates
- \bar{u} to fit estimates of the value of a life year (!)

Data for each country on:

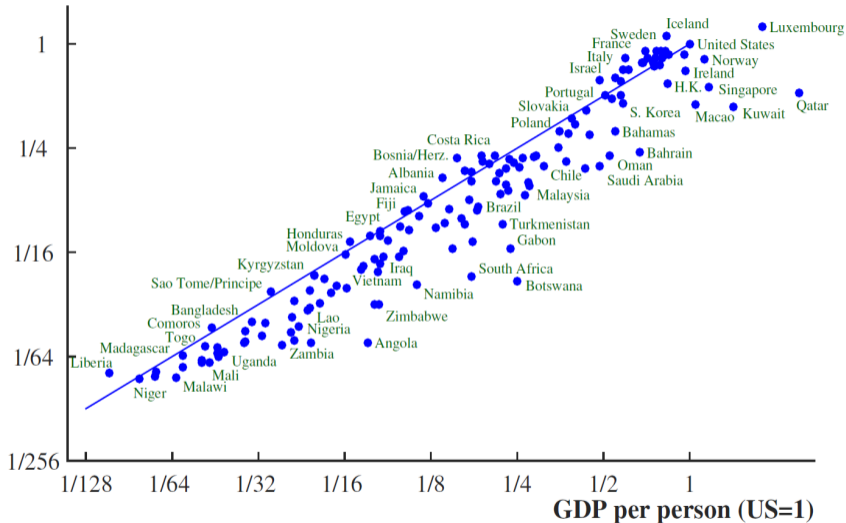
- Life expectancy e
- Mean consumption \bar{c}
- Mean leisure \bar{l}
- Consumption inequality σ

Findings on welfare vs. GDP

- $\text{corr}(\ln \lambda_i, \ln y_i/y_{us}) > 0.9$
- Mean absolute deviation $\sim 35\%$ is economically significant
- Europe is closer to the U.S. — higher life expectancy and leisure and lower inequality
- Developing countries are farther behind (life expectancy, inequality)
- Rising life expectancy boosts growth from 2% to 3%

These facts generalize to using household micro data for 13 countries.

Welfare, λ



The ratio of Welfare to Income

